

Appendix 1:Pictures of prime numbers for complex UFD

The pictures show the quadratic character and a picture of **prime numbers** and **units** for the complex quadratic fields whose domain of integers is a unique-factorization domain, namely

the fields of discriminant congruent 0 modulo 4:

$$\mathbb{Q}(\sqrt{-1}), \mathbb{Q}(\sqrt{-2})$$

and the fields of discriminant congruent 1 modulo 4:

$$\mathbb{Q}(\sqrt{-3}), \mathbb{Q}(\sqrt{-7}), \mathbb{Q}(\sqrt{-11}), \mathbb{Q}(\sqrt{-19}), \mathbb{Q}(\sqrt{-43}), \mathbb{Q}(\sqrt{-67}), \mathbb{Q}(\sqrt{-163}).$$

At the top, each picture mentions the field, $\mathbb{Q}(\sqrt{r})$, and displays its quadratic character (as far as space allows).

In the pictures, rational integers are placed on the x-axis and numbers of the form \sqrt{r} times rational integers on the y-axis.

When $d \equiv 0$ modulo 4, we use a square grid, otherwise a staggered grid, where the grid points form roughly equilateral triangles.

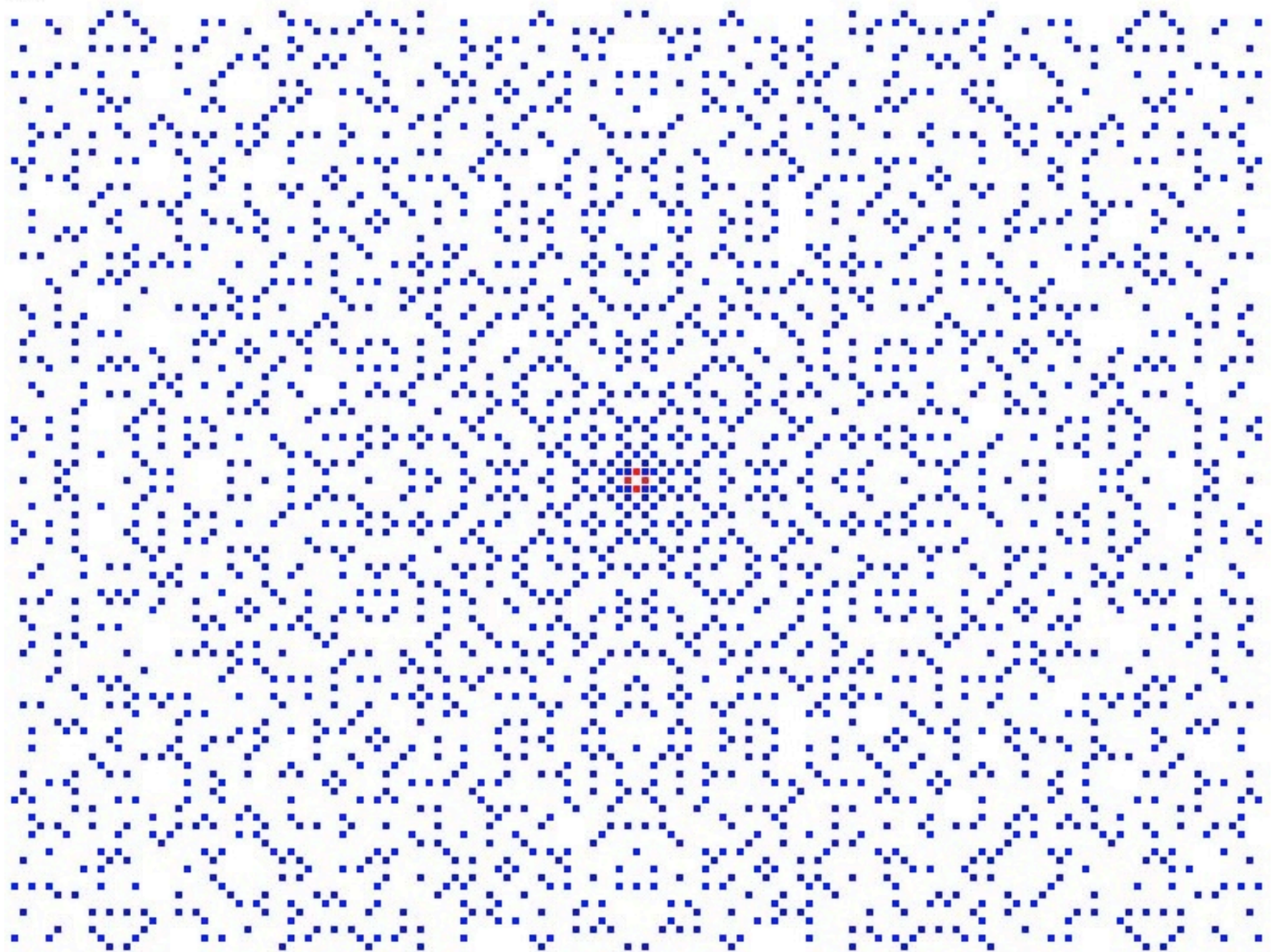
$Q(\sqrt{-1})$

chi

prime numbers

units

0+0-



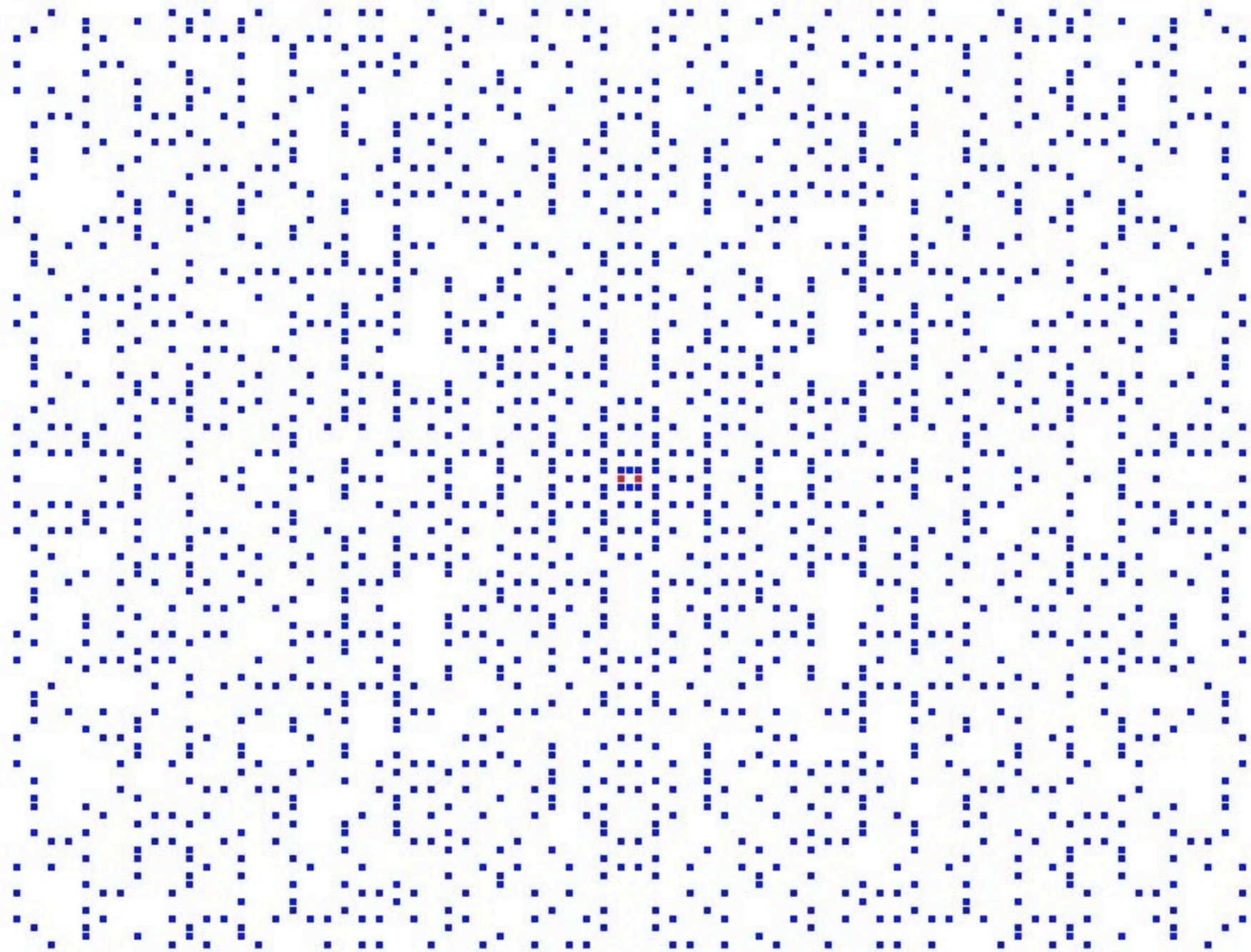
$Q(\sqrt{-2})$

chi

prime numbers

units

0+0+0-0-



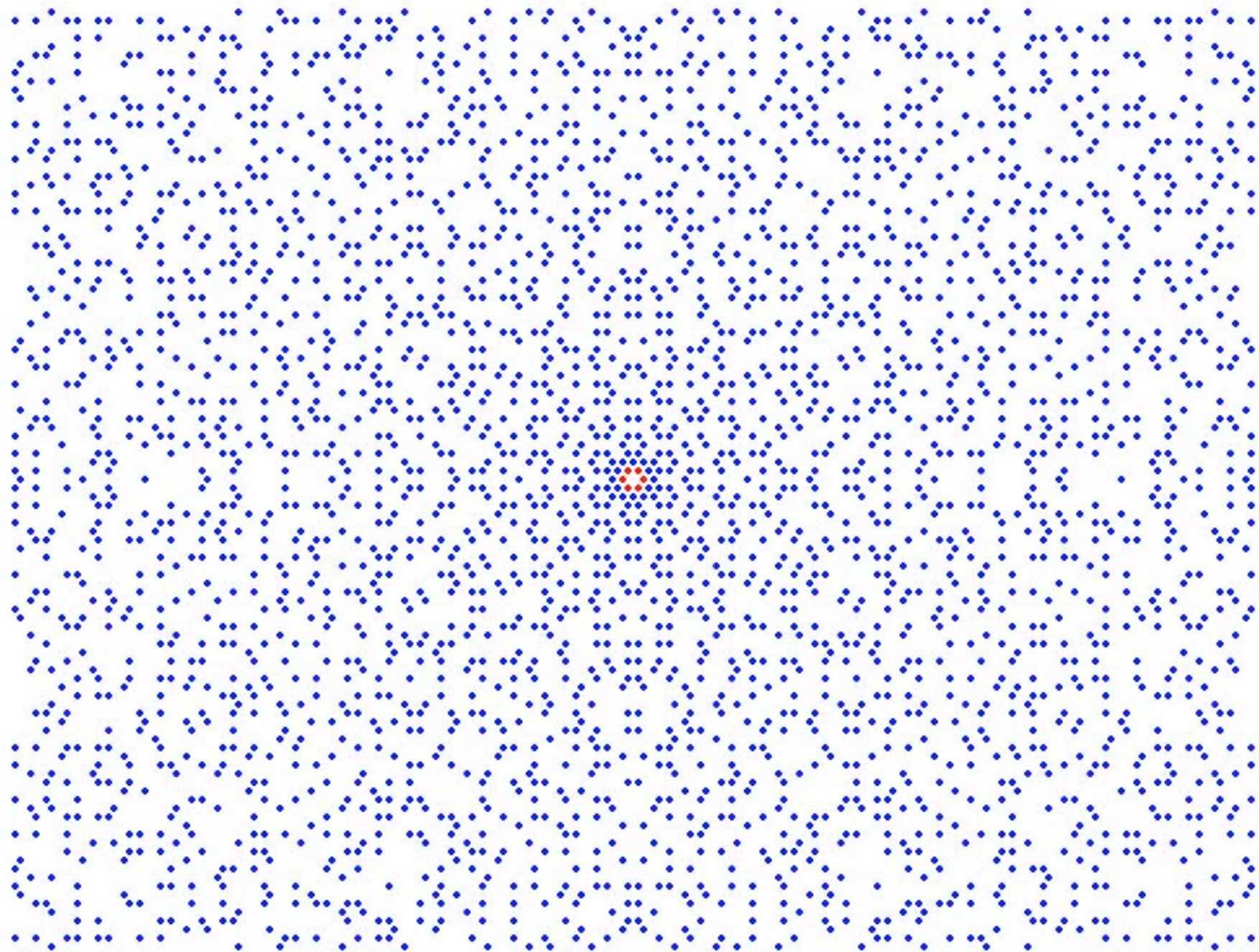
$Q(\sqrt{-3})$

chi

prime numbers

units

0+-



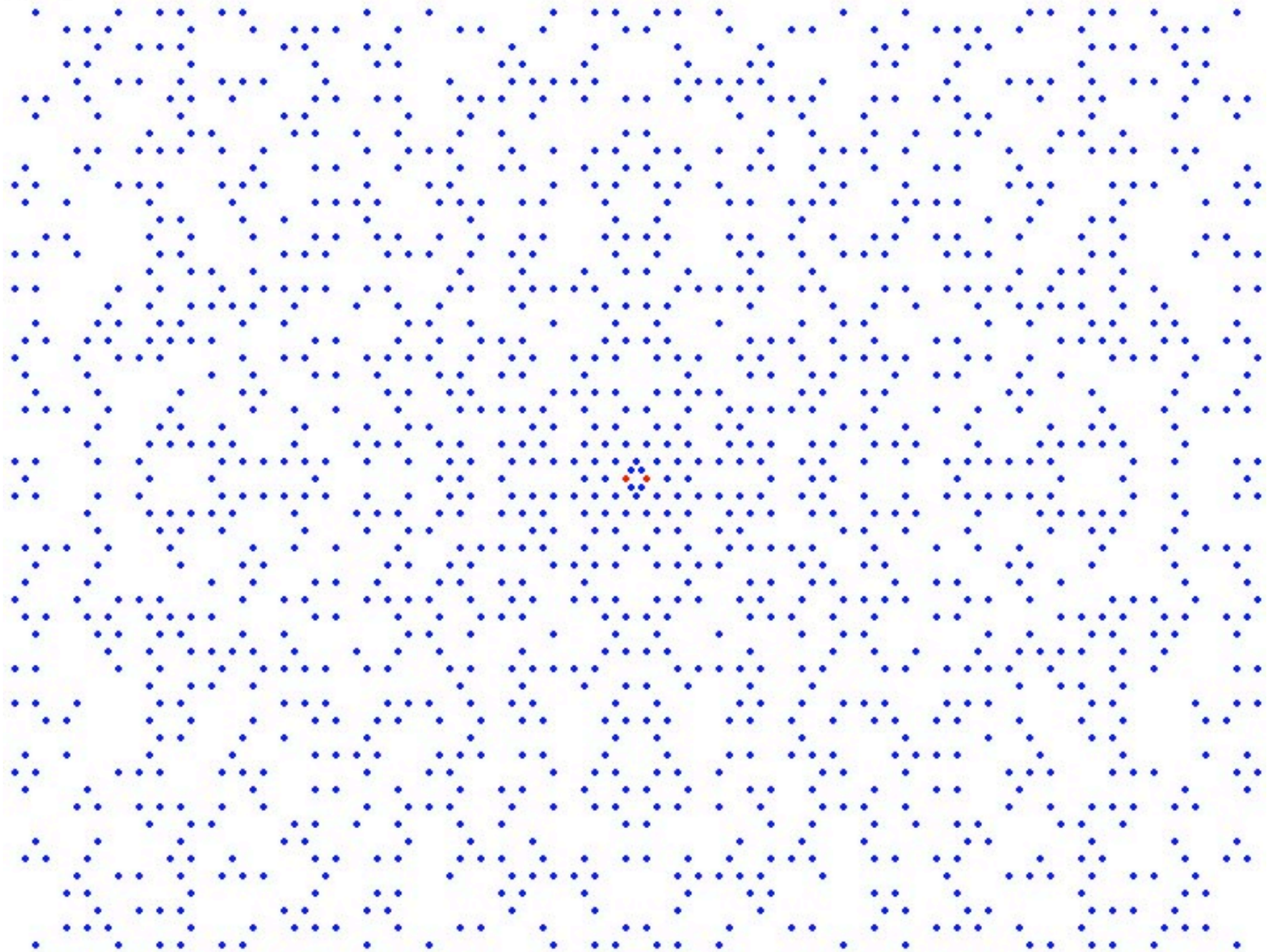
$Q(\sqrt{-7})$

chi

prime numbers

units

0++++--



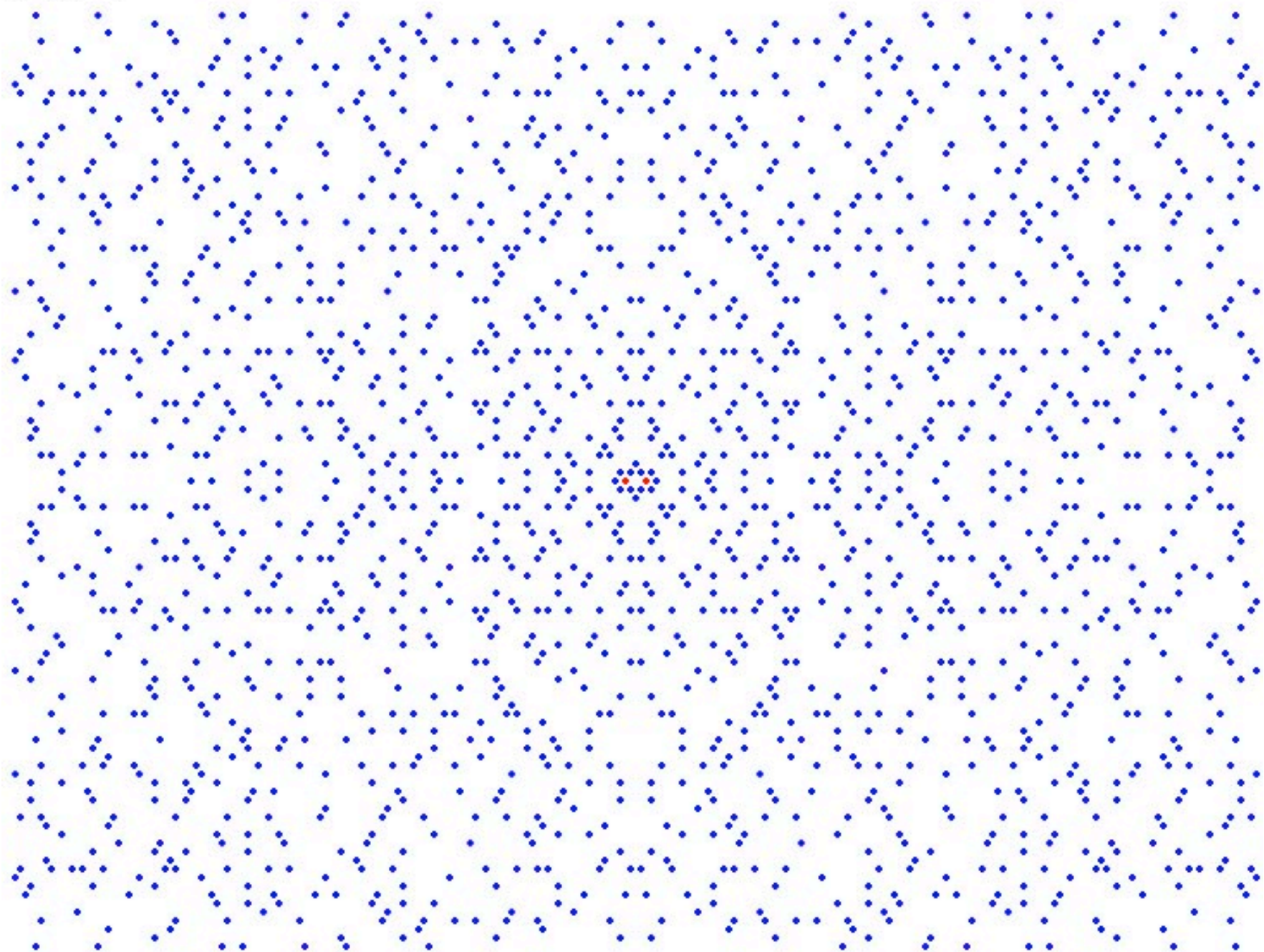
$Q(\sqrt{-11})$

chi

prime numbers

units

0+-----+



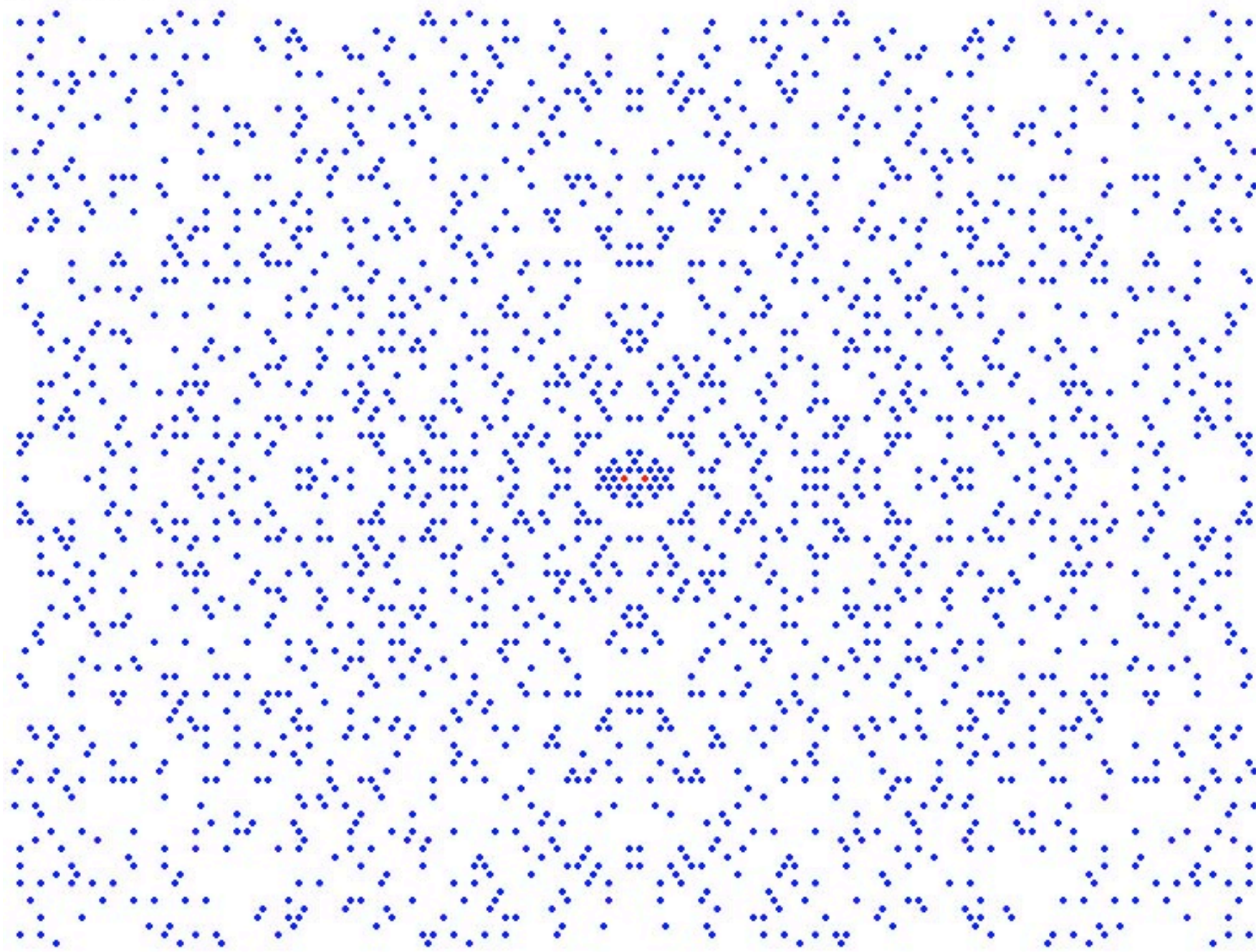
$Q(\sqrt{-19})$

chi

prime numbers

units

0+-----+



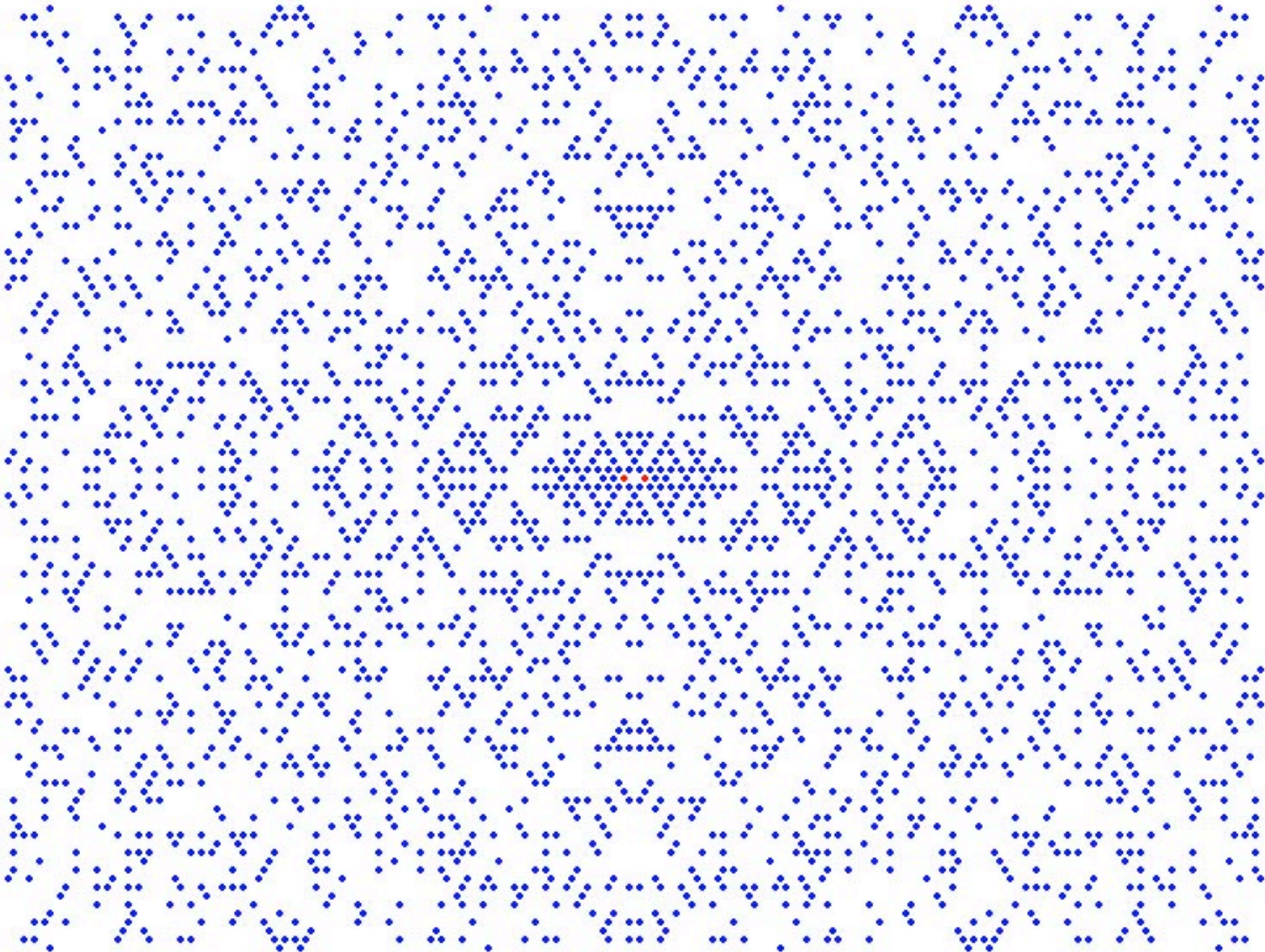
$Q(\sqrt{-43})$

chi

prime numbers

units

0+---++---++---++---++---++---++---++---++---++---++---++---++



$Q(\sqrt{-163})$

chi

prime numbers

units

