Computational Complexity

Exercise Session 3

Exercise 1. Is there an oracle such that, relative to this oracle, ...? If so, then give such an oracle and prove that it works. If not, prove why not.

- (a) $DTIME(n^2) = DTIME(n^3)$
- **(b)** $\mathsf{DTIME}(n^2) \neq \mathsf{DTIME}(n^3)$
- (c) P = coNP
- (d) $P \neq coNP$

Exercise 2. Show that if $NTIME(n) \subseteq DTIME(n)$, then P = NP.

- NTIME(n) can be characterized as the set of all decision problems that can be verified in linear time with a linear-size certificate. That is, $A \in \mathsf{NTIME}(n)$ if and only if there is a linear-time Turing machine \mathbb{M} and a constant c such that for all $x \in \{0,1\}^*$ it holds that $x \in A$ if and only if there exists some $u \in \{0,1\}^{c \cdot |x|}$ such that $\mathbb{M}(x,u) = 1$.
- *Hint:* Use a padding argument.