Errata and comments for the book Special functions

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These are errata and comments for the (very slightly corrected) 2000 softcover version of the book

G. E. Andrews, R. Askey and R. Roy, *Special Functions*, Cambridge University Press, 1999, ISBN 0-521-62321-9.

p.ix, 7.4: Replace "Bieberback" by "Bieberbach".

**p.39, fourth line from below**: Replace x(1-x) by  $x(1-x)^{-1}$ .

**p.40**: It is confusing to write  $\chi \eta \neq e$  in line 4 and write  $\chi \eta \neq id$  in line 8.

**p.53, Exercise 34**: Replace  $a^{p-1/2}$  by  $a^{(p-1)/2}$ .

**p.53, Exercise 36(a)**: Replace  $\left(-\frac{1}{p}\right)$  by (the Legendre symbol)  $\left(\frac{-1}{p}\right)$ .

p.94, Section 2.5:

Better call this Section "Contiguous relations and Jacobi polynomials".

**p.99, (2.5.13)**: Replace  $\frac{d^n}{dx^n}$  by  $\frac{d^n}{du^n}$ .

**p.99, Remark 2.5.1**:  $(5.13) \rightarrow (2.5.13)$ 

**p.101**, three lines below (2.5.17):  $T_x(x) \to T_n(x)$ 

**p.108, 7th line**: Replace (k - m + n) by (k + m - n).

**p.110, Proof of Theorem 2.8.1**: In the formula on the second line of the proof insert a minus sign at the beginning of the right-hand side.

**p.111, fourth line from below**: Replace  $\int_a^{t_{n-1}}$  by  $\int_a^{t_{n-2}}$ .

**p.115, Exercise 4(a)**:  $\frac{1}{2}((1+x)^n + (1-x)^n) \to \frac{1}{2}((1+x)^{n+1} + (1-x)^{n+1})$ 

**p.121, Exercise 39(b)**: On the third line replace  $+\frac{x(1-y)}{y(1-x)}$  by  $+\text{Li}_2\left[\frac{x(1-y)}{y(1-x)}\right]$ .

Also replace on that line  $\log 2y$  by  $\log^2 y$ .

p.145, Corollary 3.4.3: This is also a terminating case of (2.2.10).

**p.146, Proof of Theorem 3.4.4, 1.7**: The numerator should have additional factors  $(-1)^r(a-b-c+1)_r$ .

**p.156**, **l.2**: Replace "Theorem 3.3.1" by "Theorem 3.3.3".

**p.169, 6th line from below**: Replace  $\frac{ab(1-n)}{c(2-n+a+b-c)}$  by  $\frac{ab(-n)}{c(1-n+a+b-c)}$ .

**p.169, 5th line from below**: Replace  $\frac{(2-n)ab}{c(3-n+a+b-c)}$  by  $\frac{(1-n)ab}{c(2-n+a+b-c)}$ .

p.177, Exercise 3(b): The Gamma quotient on the right-hand side should be

$$\frac{\Gamma(a + \frac{3}{4})\Gamma(1/2)}{\Gamma((2a+3)/4)\Gamma((a+1)/2)}$$

**p.201, line after (4.5.9)**: Replace x = 1/2 by a = 1/2, and replace  $\alpha^2 = 1/a$  by  $\alpha = 1/3$ .

**p.253, Theorem 5.4.1**: Even better, the Theorem holds with on 1.3 [a, b] being replaced by (a, b). Then also make this replacement on 1.1 of the Proof.

**p.300, Remark 6.4.1**: Write that the expression with the *n*-th derivative is equal to  $P_n^{(\alpha,\beta)}(x)$  and observe that this is the Rodrigues formula (2.5.13') for Jacobi polynomials.

**p.306**, **(6.4.26)**: Replace  $x/\lambda$  by  $x/\lambda^{\frac{1}{2}}$ .

p.344, Exercise 27: Refer for the Rodrigues formula to (2.5.13′).

**p.362, (7.1.14)**: The ratio of shifted factorials  $\frac{(\beta+1)_n}{(\alpha+\beta+2)_n}$  right after the equation mark should be deleted.

p.484, third line after (10.0.8):

Replace y(xy) = (yx)y = q(xy)y by (xy)x = x(yx) = qx(xy).

**p.495, Proof of Theorem 3.3.3**: This is essentially the proof given in Appendix B of Koornwinder [1990].

**p.500, (10.4.8) and p.501, l.6**: In the denominator after the product sign replace  $(1-q)^{2n+1}$  by  $(1-q)^{2n-1}$ .

**p.527**, (10.11.1): In the first line replace  $(\beta;q)_n$  by  $(\beta;q)_k$ .

**p.589, line 7**: This math equation should be labelled by equation number (12.3.8). Reference to (12.3.8) is later made on p.591, Exercise 6.

**p.627**, Exercise 2, l.3:  $\frac{B_j}{j} o \frac{B_j}{j!}$ 

p.646, reference to Gegenbauer: Replace 1875 by 1874.

 $\mathbf{p.660} \text{:}\ \mathrm{Add}\ \mathrm{the}\ \mathrm{subject}\ \mathrm{index}\ \mathrm{item:}$ 

Legendre symbol, 53

**p.663**: Insert after  $(a;q)_n$  the symbol index item:  $(\frac{a}{p})$ , 53